

2.0 NUMERICAL PROCESSES (2) THEORY OF LOGARITHMS & INDICES

OBJECTIVES

1. Express statements given in index form (such as $81 = 3^4$) as an equivalent logarithms statement ($\log_3 81 = 4$).
2. Evaluate expression given in logarithms form.
3. Note the equivalence between the laws of indices and the law of logarithms
4. Recall and use the law of logarithms to simplify and/or evaluate given expression without the use of logarithm table.

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5. Use logarithms table for the purpose of calculation.

2.1 LAW OF LOGARITHMS & INDICES

The three fundamental law of indices can be stated in their equivalent logarithms form;

1. In indices: $Y^a \times Y^b = Y^{a+b}$ (Note ^ means Raise to power)

* In Logarithms: $\text{Log}(MN) = \text{Log } M + \text{Log } N$

2. In indices: $Y^a \div Y^b = Y^{a-b}$ (Note ^ means Raise to power)

* In Logarithms: $\text{Log}(M/N) = \text{Log } M - \text{Log } N$

3. In indices: $(X^a)^b = X^{ab}$ (Note ^ means Raise to power)

* In Logarithms: $\text{Log}(M^p) = p \log M$

Theory Of Logarithms And Indices

Example 1: Simplify $\text{Log } 8 + \text{Log } 5$

solution;

$$\text{Log } 8 + \text{Log } 5 = \text{Log}(8 \times 5)$$

$$\text{Ans} = \text{Log } 40$$

Example 2: Simplify $\text{Log } 9 \div \text{Log } 3$

solution;

$$\text{Log } 9 \div \text{Log } 3 = \text{Log } 9 / \text{Log } 3$$

$$\begin{aligned}
&= \log 3^2 / \log 3^1 \text{ (Note / means All over)} \\
&= 2 \log 3 / 1 \log 3 \text{ (Log 3 will cancel Log 3)} \\
&= \log 2/1 \\
&\text{Ans} = \log 2
\end{aligned}$$

Example 3: Given that $\log 2 = 0.30103$; Calculate $\log 5$ without using table

solution;

$$\begin{aligned}
\log 5 &= \log 10/2 \\
&= \log 10 - \log 2 \text{ (Note: } \log 10 = 1) \\
&= 1 - 0.30103 \\
&\text{Ans} = 0.69897
\end{aligned}$$

Example 4: Evaluate $\log_{\text{base}3}(6.84)$ to 2 d.p

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solution;

$$\begin{aligned}
&\log_3 (6.84) \\
&= \text{Let } \log_3 (6.84) = x \\
&\text{then } 3^x = 6.84 \\
&= \log(3^x) = \log(6.84) \\
&x = \log(6.84) / \log(3) \\
&x = 0.8351 / 0.4771 \\
&\text{Ans} = 1.75
\end{aligned}$$

2.2 CALCULATIONS USING LOGARITHM TABLE

Example 1: Evaluate $82.47 \times 24.85 / 209.3$

solution;

Draw a table form with "No & Log"

$$\begin{aligned}
\text{No } 82.47 &= \log 1.9163 \text{ (No means Number)} \\
\text{No } 24.85 &= \log 1.3954 \\
\text{Add together} &= 3.3117 \\
\\
\text{No } 209.3 &= \log -2.2307 \text{ (from log table)} \\
\text{Deduct } -2.2307 &\text{ from } 3.3117 \\
\\
&= 3.3117 - 2.2307 \\
&\text{Ans} = 0.9910
\end{aligned}$$

2.3 LAW OF INDICES

The following laws of indices are true for all non-zero value a, b and x

1. $X^a \times X^b = X^{a+b}$ (Note ^ means Raise to power)

2. $X^a \div X^b = X^{a-b}$ (Note ^ means Raise to power)

3. $X^0 = 1$

4. $X^{-1} = 1 / X^a$ (Note / means All over)

5. $(X^a)^b = X^{ab}$

6. $X^{1/a} = \sqrt[a]{x}$ (Note \sqrt means Square root)

7. $X^{a/b} = \sqrt[b]{x^a}$ or $(\sqrt[b]{x})^a$

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2.3.1 WORKED EXAMPLES

Example 1: Simplify $25^{1/2}$

solution;

$$25^{1/2} = \sqrt{25}$$

$$\text{Ans} = 5$$

Example 2: $4^3 \div 4^5$

solution;

$$4^3 \div 4^5 = 4^{3-5}$$

$$= 4^{-2}$$

$$= 1 / 4^2$$

$$\text{Ans} = 1/16$$

Theory Of Logarithms And Indices 4

REVISION EXERCISE

[1] Simplify $3^8 \times 3^3$

[2] Simplify $5^3 \times 5^{-1}$

[3] Express $\log 3 + \log 4$

[4] Evaluate $3\log 2 + \log 20 - \log 1.6$

[5] Simplify $\log 8 - \log 4$

[6] Simplify $\log 8 \div \log 4$

[7] Simplify $\log 4 / \log 2$

[8] Simplify $(27/48)^{3/2}$

[9] Simplify $3^6 \div 3^2$

[10] Simplify $(4/25)^{-1/2} \times (2^4) \div (15/2)^{-2}$

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